



Objective

To show that the quadrilateral formed by joining the mid-points of the adjacent sides of a quadrilateral is a parallelogram by paper folding.

Material Required

Glazed papers, pencil, a pair of scissors, glue stick and tracing paper.

Theory

1. Concept of finding mid-point of a line segment by performing a paper folding activity.
2. Properties of a parallelogram.

Procedure

1. Take any colored glazed paper.
2. Draw a quadrilateral of any dimensions on glazed paper and name it as ABCD.
3. Cut that quadrilateral from the glazed paper.
4. Now, find the mid-point of each side AB, BC, CD, DA by paper folding and name them E, F, G, H respectively as shown in fig. (i).

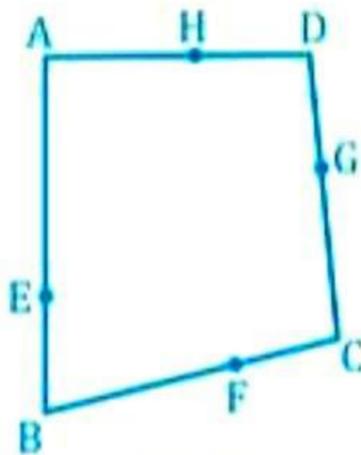


fig. (i)

5. Now, fold the figure along with EF, GF, GH and EH. Press it and then unfold it as shown in fig. (ii).

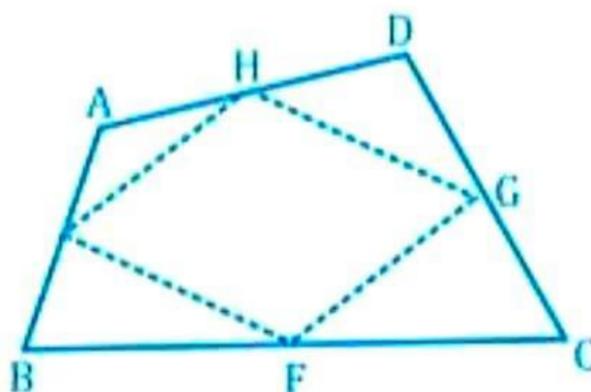


fig. (ii)

6. We will get creases along with EF, GF, GH, HE.
7. Make a replica (true copy) of EFGH (say PQRS) by using tracing paper fig. (iii)

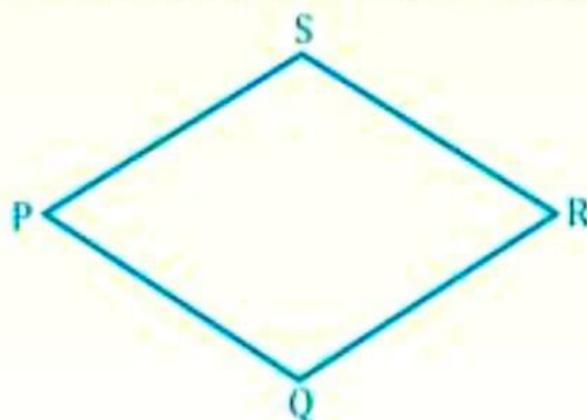


fig. (iii)

1. Cut the quadrilateral PQRS along any diagonal (say RP) [fig. (iv)].

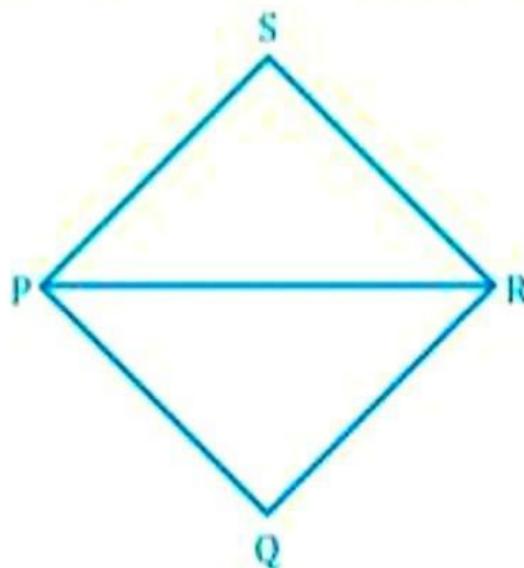


fig. (iv)

2. We will get two triangles ΔPSR and ΔPQR .
3. Now, overlap these two triangles. Two triangles coincide with each other [fig. (v)] such that side PS overlaps with QR and PQ with SR.

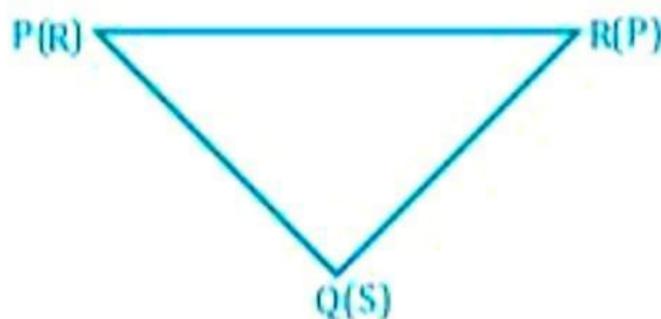


fig. (v)

Observation

We observe that two triangles coincide with each other which means two triangles are congruent to each other. In a quadrilateral, two triangles cover each other completely along any diagonal, then the quadrilateral will be a parallelogram.

- $$\therefore \Delta PQR = \Delta PSR$$
- i.e., $a r(\Delta PQR) = a r(\Delta PSR)$
- $$\therefore PQRS \text{ is a parallelogram.}$$

Result

As the replica of ΔPQR exactly covers the replica of ΔPSR

- $$\therefore PQ = RS, \quad QR = SP$$

∴ PQRS is a parallelogram.

Learning Outcome

We have verified by paper folding that the quadrilateral formed by joining mid-points of adjacent sides of a quadrilateral will be a parallelogram. We also learnt that a diagonal always divides the parallelogram into two triangles of equal areas.

Activity Time

What type of figures do you obtain?

1. If you join mid-points of the sides of a rectangle (Do it by paper folding).
2. If you join the mid-points of the sides of a square (Do it by paper folding).

Viva Voce

Q1. Name the quadrilateral in which one pair of opposite sides are equal and parallel.

Ans: Parallelogram

Q2. Name the quadrilateral formed by joining the mid-points of the sides of a quadrilateral in order.

Ans: Parallelogram

Q3. If ABCD is a rectangle, then name the quadrilateral formed by joining the mid-points of its sides in:

Ans: Rhombus (But, if ABCD is a square, then the name of the quadrilateral formed by joining the mid-points of its sides is also a square.)

Q4. What do you mean by rhombus?

Ans: A rhombus is a parallelogram with four equal sides and opposite equal angles.

Q5. Define parallelogram?

Ans: A parallelogram is a two-dimensional geometrical shape; whose sides are parallel to each other.

Q6. What do you mean by a quadrilateral?

Ans: A quadrilateral is a plane closed figure bounded by four-line segments.

Multiple Choice Questions

Q 1. In $\triangle PQR$, if S is the mid-point of PR, T lies on QR and $ST = PQ$ then:

- (a) $ST = \frac{1}{3}PQ$ (b) $ST = \frac{1}{2}PQ$ (c) $ST = PQ$ (d) None of these

Q 2. In a quadrilateral ABCD, equal diagonals AC and BD intersect at P, such that $AP = PC$, $BP = PD$ and $\angle BPC = 90^\circ$. The quadrilateral is exactly:

- (a) A parallelogram (b) A square (c) A rhombus (d) A rectangle

Q 3. Diagonals of a parallelogram ABCD intersect at O. If $\angle BOC = 90^\circ$ and $\angle BDC = 50^\circ$, the $\angle OAB$ is:

- (a) 90° (b) 50° (c) 40° (d) 10°

Q 4. The triangle formed by joining the mid-points of the sides of an equilateral triangle is:

- (a) An equilateral triangle
(b) An isosceles triangle
(c) A right-angled triangle
(d) None of these

Q 5. The diagonals of a rectangle ABCD intersect each other at O. If $\angle BOC = 44^\circ$, then $\angle OAD = ?$

- (a) 58° (b) 68° (c) 64° (d) 62°

Q 6. If bisectors of $\angle A$ and $\angle B$ of a quadrilateral ABCD intersect each other at P, that of $\angle B$ and $\angle C$ at Q, that of $\angle C$ and that $\angle D$ at R and of $\angle D$ and $\angle A$ at S, then PQRS is a:

- (a) Rectangle
(b) Rhombus
(c) Parallelogram
(d) quadrilateral whose opposite angles are Supplementary

Q 7. The triangle formed by joining the mid-points of the sides of a right triangle is:

- (a) A right triangle. (b) An obtuse-angled triangle.
(c) An isosceles triangle. (d) None of these.

Q 8. The diagonals AC and BD of a parallelogram ABCD intersect each other at the point O. If $\angle DAC = 32^\circ$ and $\angle AOB = 70^\circ$, then $\angle DBC$ is equal to:

- (a) 24° (b) 86° (c) 38° (d) 32°

Q 9. In a square, diagonals are:

- (a) Equal (b) Not equal (c) $\frac{1}{2}$ of each other (d) None of these

ANSWER KEY

1.(b)	2.(a)	3.(a)	4.(a)	5.(b)	6.(c)	7.(a)	8.(c)	9.(a)
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